



*Clinical Trials Network*



# Sensitivity Analysis for the Primary Outcome in a Drug Abuse Intervention Trial

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# Outline

- ▶ Screening, Motivational Assessment, Referral, and Treatment in Emergency Departments (SMART-ED) study
- ▶ Missing data in SMART-ED
- ▶ Distribution of the Primary Outcome in SMART-ED
- ▶ Primary Outcome Result and Sensitivity Analysis  
*Aim: To study the impact of missing data on the result of the primary outcome of this study*
- ▶ Conclusions

# Screening, Motivational Assessment, Referral, and Treatment in Emergency Departments (SMART-ED)

- ▶ National Drug Abuse Treatment Clinical Trials Network (NIDA CTN) funded Multisite Clinical Trial
- ▶ 1285 participants randomized to three treatment arms -
  1. Minimal Screening Only (MSO)
  2. Screening, assessment, and referral to treatment (SAR)
  3. SAR + brief intervention with 2 telephone follow-up booster sessions (BI-B)
- ▶ Primary Outcome – Self-reported number of days of primary drug of abuse in past 30 days at 3-month follow-up visit
- ▶ Hypotheses – 3 Multiplicity Adjusted 2-sided tests (BI-B vs SAR, BI-B vs MSO and SAR vs MSO) [Bogenschutz (2011)]

# Missing Data in SMART-ED

- ▶ Missing Data on Primary Outcome

BI-B	SAR	MSO
52/427(12.2%)	45/427(10.5%)	49/431(11.4%)

- ▶ Reasons for missing - Died, incarcerated, withdrew consent and eligible but did not return
- ▶ Impact of Missing Data on the Primary Outcome
- ▶ Graphical Sensitivity Analysis - [Hollis (2002)]

## Distribution of Number of drug use days

- ▶ Binomial Distribution - Number of drug use days in  $n$  independent days with probability  $p$

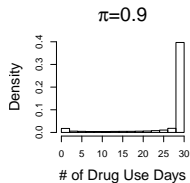
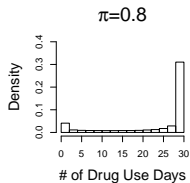
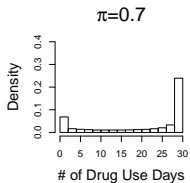
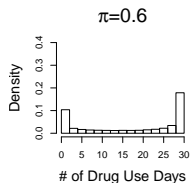
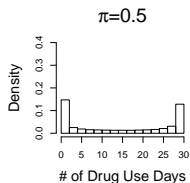
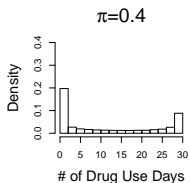
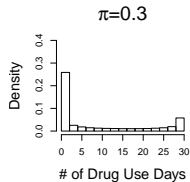
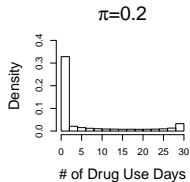
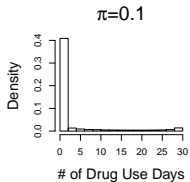
$$\mu = np \text{ and } \sigma^2 = np(1 - p)$$

- ▶ For a participant, drug use days are correlated  $\implies$  not independent
- ▶ Beta-binomial distribution is the binomial distribution in which the probability of drug use is not fixed but random and follows the beta distribution  $\implies$  correlated drug use days

$$\mu = n\pi \text{ and } \sigma^2 = n\pi(1 - \pi)[1 + (n - 1)\rho]$$

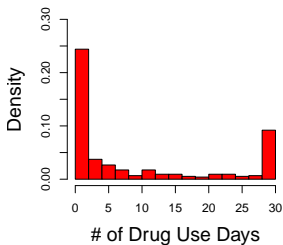
- ▶  $\pi$  (probability of drug use) and  $\rho$  (pairwise correlation between the days) are the parameters of the Beta-binomial distribution

# Beta-Binomial Distribution ( $\rho = 0.66$ , varying $\pi$ ) [VGAM]

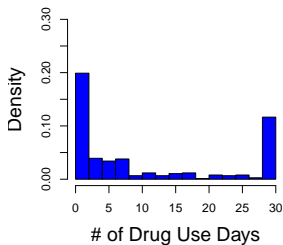


# Distribution of Primary Outcome (Observed)

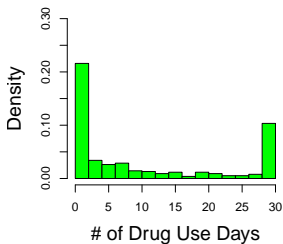
## BI-B



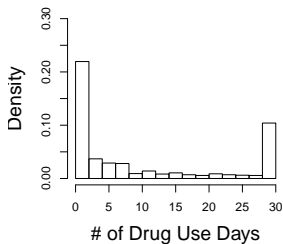
## SAR



## MSO



## Overall



# Primary Outcome Result & Sensitivity Analysis

- ▶ Primary Outcome: No statistically significant treatment effect [Bogenschutz (2014)]
- ▶ Could missing data impact this result?
- ▶ Sensitivity analysis-assume:
  - $\pi_{BIB}$  - Probability of Drug Use in Missing Ppts in BI-B arm
  - $\pi_{SAR}$  - Probability of Drug Use in Missing Ppts in SAR arm
  - $\pi_{MSO}$  - Probability of Drug Use in Missing Ppts in MSO arm
- ▶ For various combinations of these probabilities evaluate the impact of missing data on the result of the primary outcome.



## Algorithm for Sensitivity Analysis

1. For the missing participant, simulate number of drug use days using beta-binomial distribution with observed correlation  $\rho$  and probability  $\pi_{BIB}$  if the ppt is in the BI-B arm;  $\pi_{SAR}$  if in the SAR arm; and  $\pi_{MSO}$  if in the MSO arm.

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2. Analyze the complete data using primary outcome beta-binomial model and calculate the 3 multiplicity adjusted p-values for three comparisons (BI-B vs SAR, BI-B vs MSO and SAR vs MSO).

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3. Repeat the steps 1 and 2, 10 times and calculate the average obtaining 3 multiplicity adjusted p-values.

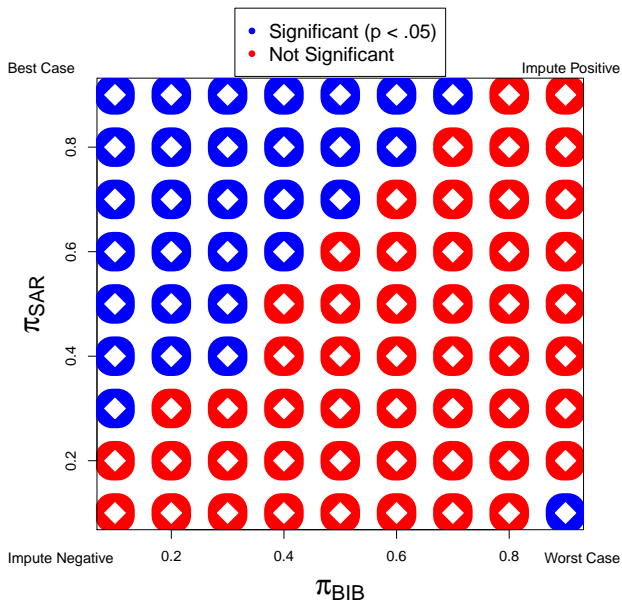
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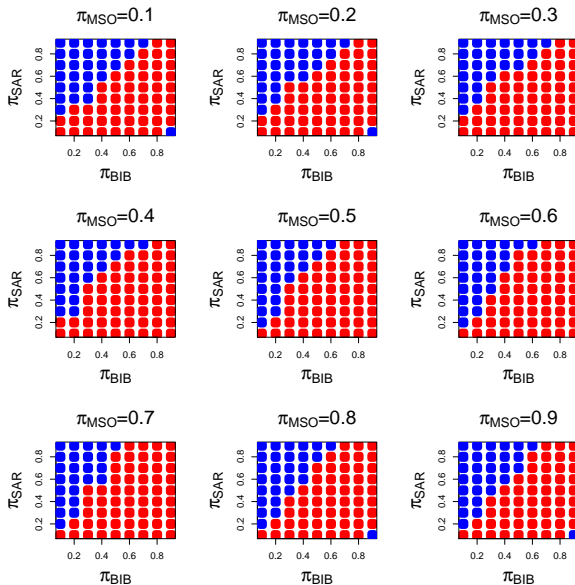
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3. Repeat the steps 1 and 2, 10 times and calculate the average obtaining 3 multiplicity adjusted p-values.
4. For a given comparison, if that average p-value from step 3 is less than 0.05 then that comparison is statistically significant, otherwise not.
5. Repeat for different combinations of  $\pi_{BIB}$ ,  $\pi_{SAR}$  and  $\pi_{MSO}$  and plot the result.

# Sensitivity Analysis Results - BI-B vs SAR ( $\pi_{MSO} = 0.1$ )

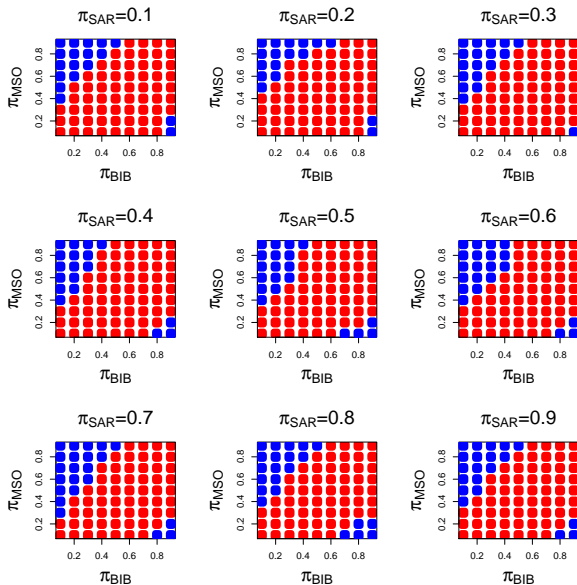


# Sensitivity Analysis Results - BI-B vs SAR



<sup>0</sup> Blue Circle - Significant, Red Circle - Not Significant

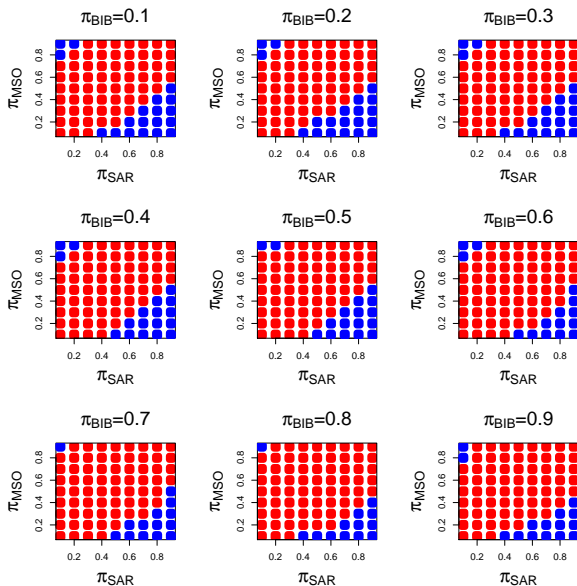
# Sensitivity Analysis Results - BI-B vs MSO



<sup>0</sup> Blue Circle - Significant, Red Circle - Not Significant



# Sensitivity Analysis Results - SAR vs MSO

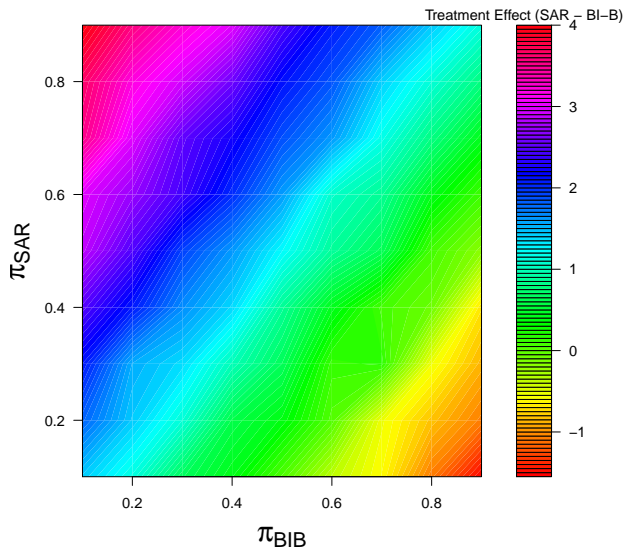


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## Conclusions

- ▶ When the assumed probability of drug use in missing participants was the same in the 2 arms, there was never a significant treatment effect between any pair of arms (more plausible scenarios).
- ▶ Best and worst case scenarios were usually but not always significant.
- ▶ Of the 729 imputation scenarios, only 32.9%, 24.1% and 20.6% were significant for comparing BI-B vs SAR, BI-B vs MSO and SAR vs MSO, respectively.
- ▶ These sensitivity analyses performed on the primary outcome provided evidence that the null result in the trial was not drastically impacted by missing data.

# Treatment Effect - BI-B vs SAR ( $\pi_{MSO} = 0.1$ )



## References

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